

**Time: 3hours** 

Max. Marks: 60

## Answer any five questions All questions carry equal marks

- 1. a) Describe the perturbing forces on a satellite orbiting the earth.
  - b) Derive the Euler Hill equation.

[4+8]

- 2. a) Derive the equations governing the changing of semi major axis and eccentricity of an orbit that can be achieved with a single impulse thrust at any point on the orbit.
  - b) The initial orbit of a satellite is  $a_1 = 5 R_e$ ,  $e_1 = 0.2$ . The final orbit is  $a_2 = 12 R_e$ . Re = 6378 km. Find the minimum eccentricity of the final orbit. [6+6]
- 3. a) Derive the equations of angular motion of a satellite.
  - b) A satellite is orbiting such that the z-axis is pointing to earth, while y-axis is normal to the orbital plane. Derive the angular velocity vector  $\omega_{RI}$  of the orbit reference frame with respect to the inertial coordinate frame, if the orbit is circular. [6+6]
- 4. For a passively controlled satellite, the equations of motion are

$$T_{dx} = I_X \ddot{\phi} + 4\omega_0^2 (I_y - I_z) \phi - \omega_0 (I_x + I_z - I_y) \dot{\psi}$$
  

$$T_{dz} = I_z \ddot{\psi} + \omega_0^2 (I_y - I_x) \psi - \omega_0 (I_z + I_x - I_y) \dot{\phi}$$
  

$$T_{dy} = I_y \ddot{\theta} + 3\omega_0^2 (I_x - I_z) \theta$$

Using Laplace Transform, find the required solutions and discuss the stability of the angular motion of the satellite. [12]

- 5. a) Discuss the active nutation control and derive the governing equations for fuel consumed during active nutation control.
  - b) A satellite has the following characteristics.  $I_x = I_y = 75 \text{ kg-m}^2$ ;  $I_z = 130 \text{ kg-m}^2$ ; Specific impulse of the fuel is 180 seconds; Torque arm of the thruster is 0.6 m; the angular velocity is 5 radians / second and the rate of energy dissipation is  $10^{-2} \text{ W}$ . What is the rate of fuel consumption required to keep the Active Nutation Control within two degrees? [6+6]
- 6. Discuss the control command laws (a) using Euler angle errors (b) using direction cosine error matrix, and (c) using the quaternion error vector. [4+4+4]
- 7. Derive the equation of motion for roll angle increment of a satellite and determine the momentum bias required for keeping the roll small. [12]
- 8. With the help of appropriate equations, describe the torque commands on a satellite and how the thruster activation time is computed. Describe PWM and PWPFM.

[12]

\*\*\*\*\*

## www.firstranker.com